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**COMPUTER SCIENCE** 

# An empirical research and comparative analysis of clustering performance for processing categorical and numerical data extracts from social media

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**ABSTRACT.** Social media has significantly influenced modern lifestyle and the way in which most of the industries operate their business. Social media data refers to the contents created by users during their social interactions in the form of text, sound, visuals, etc. It has now evolved as the major source of information for different industry verticals like retail, marketing, advertising, tourism, hospitality, education, etc. The huge volume of data resulted in the necessity for better and efficient procedures for personalized information retrieval. Traditional data mining and information retrieval techniques based on content-based and/or collaborative filtering proved computationally costly and less scalable against the volume it must deal with. Adoption of clustering techniques is a potential solution for this problem as it can minimize the amount of data required to be managed in industrial applications like recommender systems. This empirical research focuses on evaluating multiple clustering algorithms with the goal of finding an ideal solution for clustering numerical data extracted from social media sources. Three different publicly available datasets with varying number of attributes and records from tourism domain are used for the experiments conducted as part of this work.

Keywords: Collaborative filtering; clustering algorithm; data mining; recommender systems; social media.

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## Introduction

Be it any industry, social media offers quite a lot of opportunities for data scientists to perform their research. Social media interactions can be treated as a true reflection of the societal thought process on various matters (Kaplan & Haenlein, 2010). It contains huge volume of data about users and their information exchanges captured for a considerable period. Various personalized and contextualized recommender systems available across different industries leverages the predictive power of social media at large (Schoen et al., 2013; Renjith, Sreekumar, & Jathavedan, 2019; Renjith, Biju, & Mathew, 2020; Renjith, Sreekumar, & Jathavedan, 2021a, b). One of the key challenges in the area is the huge amount of data required to be processed.

Collaborative and hybrid filtering algorithms (Renjith & Anjali, 2013a; Renjith & Anjali, 2014) are extensively used by conventional recommender systems in societal contexts for forecasting probable user actions and thereby generating contextualized recommendations. The challenge associated with this approach is the huge amount of data to be processed when social media data is considered as the source of information (Jiang, Oian, Mei, & Fu, 2016; Coelho, Nitu, & Madiraju, 2018). This leads to the concept of clustering input data and process only the relevant cluster. It is important to identify the best clustering approach to be adopted considering the datasets in consideration (Estivill-Castro, 2002). This empirical study compares the quality of output and performance of multiple clustering algorithms by applying on three real time datasets collected from travel and tourism industry.

Section 2 describes the clustering concept with a quick review of various clustering algorithms and cluster evaluation techniques that are examined in this empirical study. Sections 3 reviews existing literature in this area and Section 4 describes on the methodology adopted, tools used, and datasets considered. Section 5 captures the quantitative and statistical data collated through the experiments. Section 6 discusses our observations and inferences, and Section 7 summarizes the paper along with a brief on our future research plans.

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#### **Antecedents**

#### Clustering

In the world of machine learning, clustering is the process of creating data segments within a dataset with similar elements. The aim of clustering algorithms is to form clusters with the highest intra-cluster similarity and the lowest inter-cluster similarity. Similarity is calculated in terms of a distance measure with less distance indicating more similarity. Typical distance measures in consideration include Euclidean, Cosine, Manhattan, Jaccard and Minkowski distances (Renjith & Anjali, 2013b).

## K-means algorithm

K-means (Hartigan & Wong, 1979; MacQueen, 1967) is the most commonly used partitioning clustering technique. It groups a given dataset into k dissimilar segments via an iterative process. The mean value of elements present in a cluster is labeled as the centroid. The aim of the algorithm is to ensure minimum within cluster variation for each cluster being formed. The within cluster variation at cluster level and total within cluster variation is calculated as Equation (1) and (2) respectively.

$$WCV(C_k) = \sum_{E_i \in C_k} (E_i - \mu_k)^2 \tag{1}$$

Total 
$$WCV = \sum_{k=1}^{K} WCV(C_k) = \sum_{k=1}^{K} \sum_{E_i \in C_k} (E_i - \mu_k)^2$$
 (2)

 $E_i$  is an element in cluster,  $C_k$  with  $\mu_k$  being the centroid and K being the total count of clusters formed.

K-means algorithm is considered as the simplest, less complex, easy to implement, and efficient clustering approach and thereby is the most popular one. The major challenge with this algorithm is its low tolerance towards the existence of noise or outliers. Other limitations include the prerequisite to specify the cluster count in advance, sensitiveness for initialization, and its inability to deal with non-convex cluster shapes.

#### K-medoids algorithm

K-medoids algorithm (Kaufman & Rousseeuw, 1987; Kaufman & Rousseeuw, 1990) works like k-means algorithm but differs in the logic used for determining the centroids. While k-means algorithm does not require an actual element from the dataset to mark as centroid, k-medoids algorithm always assign an element from the population as the medoid whose average dissimilarity with other cluster elements is the lowest. Partitioning around Medoids (PAM) is the most used k-medoids procedure. PAM algorithm iteratively identifies k medoids from the elements of dataset using an objective function and assign other elements to the nearest medoids for form clusters.

Compared to k-means algorithm, k-medoids algorithm is less susceptible to the presence of outliers. While k-means algorithm focuses on minimizing the total squared error, k-medoids attempts to minimize the sum of dissimilarities among entities within a cluster and its centroid. The main constraint with the algorithm is its high time complexity while comparing with k-means algorithm.

#### Clustering large applications (CLARA)

CLARA (Clustering for Large Applications) algorithm (Kaufman & Rousseeuw, 1987; Park & Jun, 2009) is an expansion of k-medoids algorithm to handle datasets having large volume. The CLARA algorithm selects a sample from the population to apply PAM procedure to determine best possible set of medoids. The goodness of these medoids are then verified against the complete population. The sampling and clustering process are repeated to minimize the sampling bias. This approach helps in reducing the limitations of PAM like lengthy processing time and high memory needs.

The major advantage of CLARA algorithm is its ability to deal with larger datasets while preserving the benefits of k-Medoids or PAM. The key drawback of the algorithm is its dependency on the sample size being chosen. Also, any probable bias in selecting the sample may influence the overall quality of the clustering process.

## **Fuzzy C-means algorithm**

Fuzzy C-means algorithm (FCM) (Bezdek, Ehrlich, & Full, 1984) is a soft clustering technique with every element in the population can belong to each cluster formed to a certain magnitude. Based on the similarity or distance of an element with the centroid of a cluster, the extent of belonging of it to the cluster is

calculated. If the element is nearer to a centroid, its belonging to the corresponding cluster will be high, of course with the cumulative membership value for an element at any point of time is kept as 100% or 1. Mathematically, the belongingness of an element in clusters can be denoted as in Equation (3).

$$\sum_{k=1}^{K} \mu_k (E_i) = 1 \tag{3}$$

K is cluster count and  $\mu_k$  is the extent of belongingness of an element,  $E_i$  in cluster,  $C_k$ .

Fuzzy C-means algorithm is the best option to select while the dataset contains overlapped clusters. As it allows partial belongings of entities in multiple clusters, the algorithm always converges. However, this results in high computational time requirements. As like k-means algorithm, FCM also has the constraint of specifying cluster count in advance and has high sensitiveness for initialization.

## **Agglomerative nesting**

Agglomerative nesting aka hierarchical agglomerative clustering (AGNES or HAC) (Kaufman & Rousseeuw, 1990; Zepeda-Mendoza & Resendis-Antonio, 2013) is the hierarchical clustering strategy which adopts a bottom-up approach. This algorithm commences with every element in the dataset as an individual cluster. At each succeeding phase, the algorithm successively merges the closest pair of clusters till one cluster remains. The algorithm has to take irreversible clustering decisions based on local patterns at each stage as it lacks global distribution details of the dataset. Agglomerative nesting is the widely used hierarchical clustering algorithm in practice.

Hierarchical clustering algorithm does not require upfront information on the cluster count. Agglomerative nesting is easy to implement and could yield best results in most of the scenarios. Major challenges include relatively high time complexity  $(O(n^2 \log n))$  and difficulty in identifying correct number of clusters from dendrogram. Also

#### Divisive analysis

Divisive Analysis aka hierarchical divisive clustering (DIANA or HDC) (Kaufman & Rousseeuw, 1990; Jayaprada, Amarapini, & Gayathri, 2014) is the hierarchical clustering strategy which adopts a top-down approach. The clustering process begins from the top with all elements considered as members of one group. This cluster is then sliced using a flat clustering algorithm like k-means. These steps are recursively performed until each element become a member of a singleton cluster.

The implementation of top-down approach is complicated in comparison with bottom-up approach as it require a separate algorithm to slice the clusters. However, this clustering model possess the advantage of having complete knowledge of the global distribution of dataset while taking clustering decisions.

## **Expectation-maximization**

The expectation-maximization (EM) clustering technique (Bouveyron, Girard, & Schmid, 2007) works like k-means algorithm, but with the key difference of not performing hard-assignment of elements to clusters and rather do a soft assignment. EM clustering algorithm determines the probability of cluster belongingness (expectation) based on probability distributions. The aim of EM clustering algorithm is to ensure maximum overall probability for the final set of clusters. The algorithm assumes that dataset is always a subset of Gaussian distribution mixture.

The EM clustering is widely used for determining the missing data in a sample. In EM algorithm the likelihood always increases with the number of iterations. It leverages both forward and backward probabilities and suffers with slow convergence to the local optima.

#### Related works

There are some good review articles available which mainly talk about the challenges and approaches to address those in the big data context. (Parker, 2012) explained the differences between large scale machine learning and standard supervised classification scenario. (Jagadish et al., 2014) articulated various challenges in leveraging the full potential of big data like inconsistency, heterogeneity, incompleteness, privacy, timeliness, visualizations, etc. (Grolinger et al., 2014) described various issues with MapReduce while handling big data. (Najafabadi et al., 2015) narrated on how data analytics problems can be tackled with the help of deep learning and the improvements required in specific areas of deep learning to perform better. (L'Heureux, Grolinger, Elyamany, & Capretz, 2017) shared a good composition of the restraints in performing

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machine learning approaches with big data and their cause-effect relationship with four dimensions of big data - i.e., volume, variety, velocity, and veracity.

(Xu & Wunsch II, 2005) did an extensive survey of clustering algorithms, but lacked on covering the big data or social media context in it. (Shirkhorshidi, Aghabozorgi, Wah, & Herawan, 2014) provided an academic review of various clustering algorithms to handle big data concerns. Other theoretical works regarding the usage of clustering algorithms in the context of big data include the literatures from (Sajana, Rani, & Narayana, 2016), (Ajin & Kumar, 2016), and (Dave & Gianey, 2016). The significant works in empirical analysis of clustering algorithms are limited. (Wei, Lee, & Hsu, 2003) conducted an experimental study of the data characteristics of CLARA, CLARANS, GACR, and GAC-RARw clustering algorithms. (Fahad et al., 2014) attempted a comparison of five candidate clustering algorithms using ten different datasets - eight of which are simulated and two are publicly available datasets used in multiple researches.

Latest studies (Shin, 2021a, b, c, d, e, f) in the area of algorithmic journalism give high focus to algorithmic trust, which can be considered as a measure of the digital affordance to algorithm based offerings. It is important to establish sufficient level of algorithmic trust before finalizing an approach in artificial intelligence based systems. It is observed that there are only a limited number of empirical analysis are conducted on clustering algorithms in the past focusing on a particular industry segment. Few attempts of this type include experimental works performed by S. Renjith et al. by using datasets from tourism domain (Renjith, Sreekumar, & Jathavedan, 2018; Renjith, Sreekumar, & Jathavedan, 2020a, b, c). Our attempt in this work is to perform an empirical analysis of the core clustering algorithms explicitly focusing on real datasets from travel and tourism domain.

# Methodology

#### **Approach**

This research is conducted using a three-stage approach as depicted in Figure 1. The same process is repeated for all datasets in consideration to arrive at the inferences.

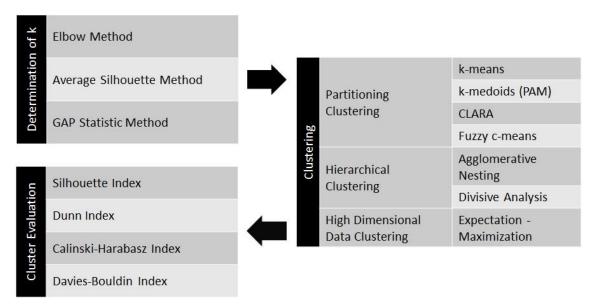


Figure 1. Three-stage research methodology adopted in this work.

#### **Determination of k**

Partitioning, hierarchical and expectation-maximization clustering techniques require to determine the optimal cluster count (k). However, determination of k is subjective and highly dependent on the similarity measures chosen and parameters considered for clustering. We chose to use the three most common algorithms to determine k - two direct methods (Elbow Method (Thorndike, 1953), Average Silhouette Method (Rousseeuw, 1987)) and one statistical testing method (GAP Statistic Method (Tibshirani, Walther, & Hastie, 2001)). Direct methods work by optimizing a criterion like intra-cluster sum of squares in Elbow Method and statistical testing method compares evidences against a null hypothesis.

### Clustering

We have experimented with four partitioning clustering algorithms (k-means (Hartigan & Wong 1979; MacQueen, 1967), k-medoids (Kaufman & Rousseeuw, 1987; Kaufman & Rousseeuw, 1990), CLARA (Kaufman & Rousseeuw, 1987; Park & Jun, 2009), and fuzzy c-means (Bezdek et al., 1984)), two hierarchical clustering algorithms (agglomerative nesting (Kaufman & Rousseeuw, 1990; Zepeda-Mendoza & Resendis-Antonio, 2013), and divisive analysis (Kaufman & Rousseeuw, 1990; Jayaprada et al., 2014)), and one model-based high dimensional data clustering algorithm (expectation - maximization (Bouveyron et al., 2007)).

#### **Cluster evaluation**

We have validated the clustering outputs using three popular internal evaluation criteria namely Silhouette Index (Rousseeuw, 1987), Dunn Index (Dunn, 1973), Calinski-Harabasz Index (Calinski & Harabasz, 1974) and Davies-Bouldin Index (Davies & Bouldin, 1979).

#### Tools used

R programming language (R Core Team, 2009; Tierney, 2012), the free open-source programming language for statistical computing and RStudio (Racine, 2011), its integrated development environment are extensively leveraged in this experimental analysis. The specific packages that are used in this research are captured in Table 1.

Package	Purpose
stats	k-means algorithm
cluster	Partition around medoids (k-medoids or PAM) and Clustering for Large Applications (CLARA) algorithms
ppclust	Fuzzy c-means (FCM) algorithm
factoextra	Agglomerative nesting (AGNES) and Divisive analysis (DIANA) algorithms
HDclassif	Expectation - Maximization algorithm (Bergé, Bouveyron, & Girard, 2012)
NbClust	Get optimal count of clusters (Charrad, Ghazzali, Boiteau, & Niknafs, 2014)
clusterCrit	Internal evaluation of clusters
stats	k-means algorithm

**Table 1.** Purpose of R packages used in the analysis.

#### Datasets used

We leveraged three real-world datasets from travel and tourism domain that are publicly available on The UCI Machine Learning Repository (Renjith & Anjali, 2014; Renjith, Sreekumar, & Jathavedan, 2018) for our experiments and recorded the results. These datasets correspond to the user interest details collated from destination reviews, ratings on attractions visited, and feedbacks provided on different point of interests from three different geographies. Subsequent sections depict more specifics of the datasets in consideration.

## Dataset 1

High level dataset description for dataset 1 is provided in Table 2. This dataset was used by the research team to evaluate collaborative filtering technique and was derived from reviews on points of interest published by 249 top contributing members of holidayiq.com in 2014 (Renjith & Anjali, 2014). Reviews spanning across 6 categories mentioned in Table 2 about the point of interests located in South India were collated and the number of reviews per category per reviewer is captured. Personally identifiable information (PII) is masked in the dataset to ensure anonymity.

#### Dataset 2

High level dataset description for dataset 2 is provided in Table 3. Dataset 2 is collated by crawling TripAdvisor.com (Renjith, Sreekumar, & Jathavedan, 2018). Destination reviews falling under 10 categories specified in Table 3 across East Asian countries are captured. Each user rating is recorded in a scale of 0 to 4 and the average rating is calculated per category per user. Personally identifiable information (PII) is not captured in the dataset.

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Table 2. I	Dataset	description	for dataset	1.
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Description	User interest information derived from traveler reviews on tourist destinations from South India
Record Count	249
Count of Attributes	1 user attribute and 6 user interest attributes
	Attrib01: Unique user identification number
	Attrib02: Count of reviews published on sports facilities.
	Attrib03: Count of reviews published on religious destinations.
Details of Attributes	Attrib04: Count of reviews published on natural bodies like beach, lake, etc.
	Attrib05: Count of reviews published on cinemas, exhibitions, etc.
	Attrib06: Count of reviews published on shopping destinations.
	Attrib07: Count of reviews published on parks or picnic destinations.

**Table 3.** Dataset description for dataset 2.

Description	User interest information derived from destination reviews on tourist destinations across East Asian countries
Record Count	980
Count of Attribute	s 1 user attribute and 10 feedback attributes
	Attrib01 : Unique user identification number
	Attrib02 : Avg. user rating on art galleries
	Attrib03 : Avg. user rating on dance clubs
	Attrib04 : Avg. user rating on juice bars
	Attrib05 : Avg. user rating on restaurants
Details of Attribute	Attrib06 : Avg. user rating on museums
	Attrib07 : Avg. user rating on resorts
	Attrib08: Avg. user rating on parks/picnic spots
	Attrib09 : Avg. user rating on beaches
	Attrib10 : Avg. user rating on theaters
	Attrib11: Avg. user rating on religious institutions

#### Dataset 3

High level dataset description for dataset 3 is provided in Table 4. Dataset 3 is collated by taking user ratings from Google reviews (Renjith, Sreekumar, & Jathavedan, 2018). Ratings on points of interest from 24 categories mentioned in Table 4 throughout Europe are captured. Average user rating per category is calculated and recorded (Google ratings range from 1 to 5). No personally identifiable information (PII) is stored in our systems.

#### Determination of k

Three indices considered by us in this paper to determine optimal cluster count (K) are Elbow Method, Average Silhouette Method, and one GAP Statistic Method. We used the functions available in the R package factoextra for capturing and plotting the criteria considered.

#### **Empirical research**

## **Elbow method**

Elbow method (Thorndike, 1953) is proposed based on the clustering goal of achieving the lowest total within-cluster sum of square (Total WSS). This approach calculates the 'Total WSS' as a function of cluster count for the dataset in consideration. The optimal cluster count, K' is determined through iteration when there is not much improvement to 'Total WSS' by choosing (K'+1) clusters. Mathematically, the 'Total WSS' is represented as Equation (4).

$$Total\ WSS = f(k) = \sum_{k=1}^{K} \sum_{E_i \in C_k} (\mu_k - E_i)^2$$
(4)

K is the number of clusters considered in each iteration and  $E_i$  is an element of the cluster,  $C_k$  having centroid,  $\mu_k$ .

The plot of 'Total WSS' against number of clusters form the shape of an elbow and hence the approach is named so. Figure 2 represents the elbow plots for the three datasets considered in this paper.

**Table 4.** Dataset description for dataset 3.

Description	Average user rating on different types of tourist destinations from Europe
Record Count	5456
Count of Attributes	1 user attribute and 24 rating attributes
	Attrib01 : Unique user identification number
	Attrib02: Avg. user feedback score for churches
	Attrib03: Avg. user feedback score for resorts
	Attrib04 : Avg. user feedback score for beaches
	Attrib05 : Avg. user feedback score for parks
	Attrib06 : Avg. user feedback score for theatres
	Attrib07: Avg. user feedback score for museums
	Attrib08 : Avg. user feedback score for malls
	Attrib09 : Avg. user feedback score for zoos
	Attrib10: Avg. user feedback score for restaurants
	Attrib11 : Avg. user feedback score for pubs/bars
	Attrib12: Avg. user feedback score for local services
Details of Attributes	Attrib13 : Avg. user feedback score for burger/pizza shops
	Attrib14 : Avg. user feedback score for hotels/other lodgings
	Attrib15: Avg. user feedback score for juice bars
	Attrib16: Avg. user feedback score for art galleries
	Attrib17: Avg. user feedback score for dance clubs
	Attrib18: Avg. user feedback score for swimming pools
	Attrib19 : Avg. user feedback score for gyms
	Attrib20 : Avg. user feedback score for bakeries
	Attrib21 : Avg. user feedback score for beauty & spas
	Attrib22 : Avg. user feedback score for cafes
	Attrib23 : Avg. user feedback score for viewpoints
	Attrib24: Avg. user feedback score for monuments
	Attrib25 : Avg. user feedback score for gardens

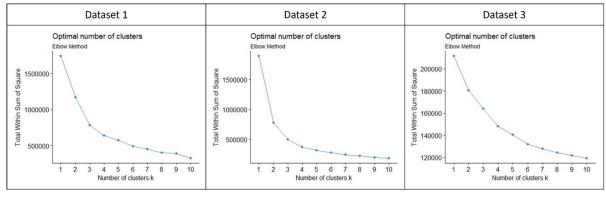


Figure 2. Determination of optimal cluster count using Elbow method.

## Average silhouette method

Average silhouette method (Rousseeuw, 1987) is based on the clustering objective of having maximum Average Silhouette. This approach calculates the 'Average Silhouette' as a function of cluster count for the dataset in consideration. The optimal cluster count, K' is identified when the maximum value is achieved for 'Average Silhouette'. Mathematically, the 'Average Silhouette' is represented as Equation (5).

Average Silhouette = 
$$f(K) = \frac{1}{K} \sum_{k=1}^{K} S_k$$
 (5)

K is the number of clusters considered in each iteration and  $S_k$  is the cluster mean Silhouette, which is calculated through steps Equation (6) to (10).

For each element,  $E_i$  determine the average dissimilarity,  $\alpha(i)$  with all other elements of the cluster,  $C_k$  to which it belongs to

$$\alpha(i) = \frac{1}{n_{k-1}} \sum_{i' \in I_k \text{ and } i' \neq i} d\left(E_i, E_{i'}\right) \tag{6}$$

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For all other clusters,  $C_{k'}$  to which element,  $E_i$  does not belong to, determine the average dissimilarity,  $\delta(E_i, C_{k'})$  of the element,  $E_i$  to the elements of every other clusters,  $C_{k'}$ .

$$\delta(E_i, C_{k'}) = \frac{1}{n_{k'}} \sum_{i' \in I_{k'}} d(E_i, E_{i'}) \tag{7}$$

The dissimilarity between element  $E_i$  and the nearest cluster to which it does not belong to,  $\beta(i)$  is computed as

$$\beta(i) = \min_{k' \neq k} \delta(E_i, C_{k'}) \tag{8}$$

The Silhouette width for the element  $E_i$  is calculated as

$$s(i) = \frac{\beta(i) - \alpha(i)}{\max(\alpha(i), \beta(i))} \tag{9}$$

The cluster mean Silhouette,  $S_k$  is computed as

$$S_k = \frac{1}{n_k} \sum_{i \in I_k} s(i) \tag{10}$$

Figure 3 represents the Average silhouette plots of the three datasets considered in this paper.

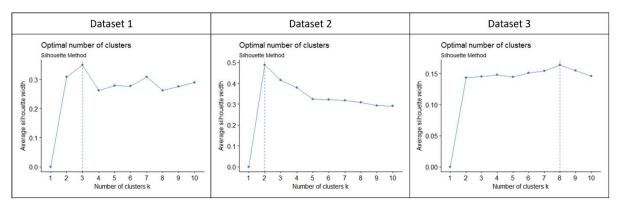


Figure 3. Determination of optimal cluster count using Average silhouette method.

## Gap statistic method

Gap statistic method (Tibshirani, Walther, & Hastie, 2001) calculates 'total intra-cluster variation' as a function of cluster count for the dataset and compares it against anticipated values for null reference distribution of all the elements in the dataset. The optimal cluster count, K' is calculated as in Equation (11) to (13).

$$K' = \min(k), \text{ such that } Gap(k) \ge Gap(k+1) - s_{k+1}$$
(11)

$$Gap_n(k) = E_n^* \{ \log W_k \} - \log W_k \tag{12}$$

Simulation Error, 
$$s_k = \sqrt{1 + \frac{1}{B \, sd(k)}}$$
 (13)

 $W_k$  is the variance quantity, B is the Monte Carlo and sd(k) is the standard deviation. Figure 4 represents the Gap Statistic plots for the three datasets considered in this paper.

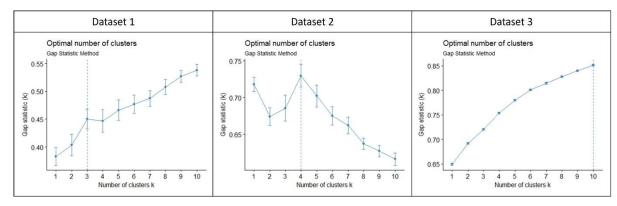


Figure 4. Determination of optimal cluster count using Gap Statistic method.

## Clustering

Figures 5, 6, 7, 8, 9, 10 and 11 depicts the two dimensional plots of the resulting clusters on the three datasets in consideration.

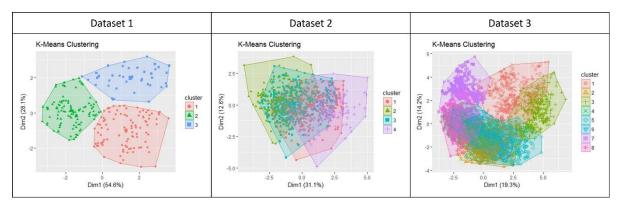


Figure 5. k-means clustering of three datasets in consideration.

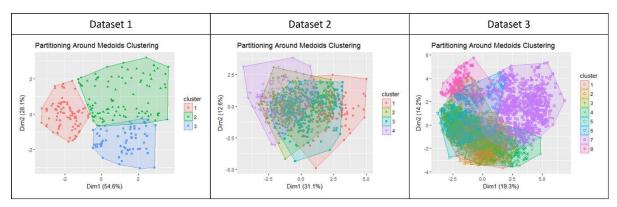
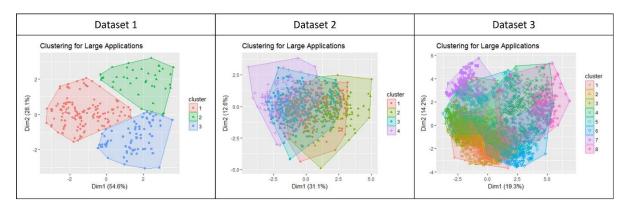


Figure 6. k-medoids (PAM) clustering of three datasets in consideration.



 $\textbf{Figure 7.} \ \textbf{CLARA} \ \textbf{clustering of three datasets in consideration.}$ 

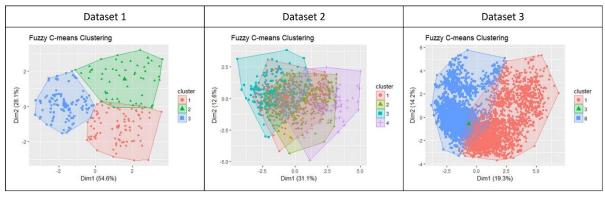


Figure 8. Fuzzy c-means clustering of three datasets in consideration.

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Figure 9. Agglomerative hierarchical clustering of three datasets in consideration.

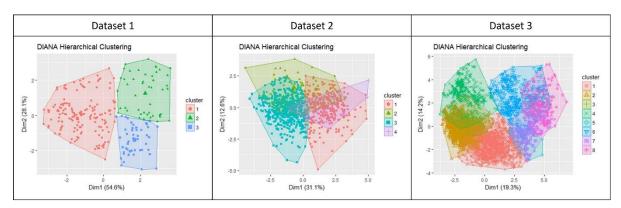


Figure 10. Divisive Hierarchical clustering of three datasets in consideration.

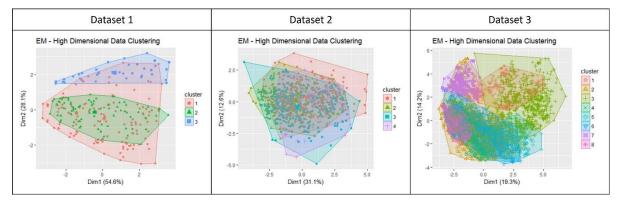


Figure 11. High Dimensional Data Clustering (using Expectation - maximization) of three datasets in consideration.

#### **Cluster evaluation**

Cluster evaluation is the process of measuring the quality or goodness of the clustering process. The key approach in evaluating clusters is internal evaluation, where the clustering accuracy is measured as a quality index. There are multiple internal evaluation measures proposed by various researchers and the key approaches include Silhouette index (Rousseeuw, 1987), Dunn index (Dunn, 1973), Calinski-Harabasz index (Calinski & Harabasz, 1974) and Davies-Bouldin index (Davies & Bouldin, 1979). Tables 5, 6 and 7 summarize complete set of observations captured using the R package clusterCrit for each clustering experiments on all three datasets.

Rule k-medoids CLARA **FCM AGNES** DIANA Index k-means Ball-Hall maximum difference 3108.694 3408.315 3286.101 3316.374 3855.931 3670.431 5023.637 Banfeld-Raftery minimum 1997.632 2012.631 2015.598 2003.073 2083.153 2043.688 2136.191 0.109289 0.106268 0.111697 0.202202 0.132742 0.360147 minimum 0.156458 Calinski-Harabasz maximum 149.7532 126.6908 137.2106 145.1667 66.9698 110.8282 35.9588 1.032207 Davies-Bouldin minimum 1.039654 1.169786 1.071810 1.352548 1.104113 2.913632

**Table 5.** Cluster evaluation details for dataset 1.

Det Ratio	minimum difference	-9.2397	-7.3837	-8.4748	8.5860	-6.3090	7.9184	4.6422
Dunn	maximum	0.053582	0.047632	0.065719	0.044738	0.084775	0.056638	0.026759
Baker-Hubert Gamma	n maximum	0.749760	0.639956	0.753406	0.743996	0.569685	0.700797	0.240393
G plus	minimum	0.058491	0.081130	0.059737	0.058632	0.107293	0.074145	0.182447
GDI	maximum	0.053582	0.047632	0.065719	0.044738	0.084775	0.056638	0.026759
GDI	maximum	0.312923	0.234861	0.380998	0.253149	0.413514	0.351454	0.152812
GDI	maximum	0.108711	0.081032	0.132948	0.088336	0.143536	0.122316	0.053064
GDI	maximum	1.010285	1.125364	1.056989	1.056989	1.014902	1.010285	0.806539
GDI	maximum	5.900093	5.548888	6.127773	5.980983	4.950473	6.269047	4.605828
GDI	maximum	2.049721	1.914494	2.138273	2.087042	1.718371	2.181810	1.599364
GDI	maximum	0.492003	0.548003	0.524025	0.517120	0.494528	0.512719	0.349893
GDI	maximum	2.873311	2.702065	3.037971	2.926124	2.412203	3.181536	1.998103
GDI	maximum	0.998202	0.932274	1.060093	1.021060	0.837306	1.107267	0.693837
GDI	maximum	0.399303	0.445758	0.419673	0.423407	0.356309	0.408797	0.124991
GDI	maximum	2.331941	2.197923	2.433007	2.395849	1.738001	2.536676	0.713777
GDI	maximum	0.810128	0.758334	0.848993	0.836023	0.603282	0.882837	0.247858
GDI	maximum	0.191100	0.215337	0.221162	0.210940	0.226125	0.229717	0.211111
GDI	maximum	1.116031	1.061772	1.282158	1.193606	1.102987	1.425447	1.205570
GDI	maximum	0.387715	0.366336	0.447406	0.416504	0.382860	0.496097	0.418632
Ksq DetW	maximum difference	5.58.E+28	6.98.E+28	6.09.E+28	-6.01.E+28	8.17.E+28	-6.51.E+28	-1.11.E+29
Log Det Ratio	minimum difference	NaN	NaN	NaN	535.384	NaN	515.229	382.264
Log SS Ratio	minimum difference	0.196804	0.029565	0.109333	0.165698	-0.607943	-0.104203	-1.229810
McClain-Rao	minimum	0.569550	0.612671	0.571827	0.569349	0.665627	0.600086	0.836456
PBM	maximum	3953.264	2874.049	3889.564	3352.529	3227.626	2942.661	1623.846
Point-Biserial	maximum	-27.09968	-23.18306	-27.97701	-26.60413	-21.69544	-26.58485	-9.37878
Ray-Turi	minimum	0.316503	0.344230	0.328744	0.313391	0.575935	0.352242	3.990921
Ratkowsky-Lance	maximum	0.431878	0.414224	0.419599	0.429530	0.370675	0.416439	0.244542
Scott-Symons	minimum	NaN	NaN	NaN	7472.943000	NaN	NaN	NaN
SD	minimum	0.444982	0.494001	0.463430	0.475443	0.595929	0.560087	0.745296
SD	minimum	0.016679	0.016177	0.016581	0.016061	0.021395	0.015918	0.055505
S Dbw	minimum	0.444982	0.827334	1.606287	Inf	1.462595	5.810087	1.678630
Silhouette	maximum	0.360524	0.305478	0.353079	0.323384	0.317772	0.311686	0.148054
Tau	maximum	0.512631	0.429613	0.524413	0.503537	0.402293	0.493362	0.166613
Trace W	maximum difference	783411.6	855770.7	821173.4	796810.6	1124800.0	913824.9	1344235.0
Trace WiB	maximum difference	4.160582	3.467845	3.866838	3.962628	3.601713	4.173832	2.394011
Wemmert-Gan carski	maximum	0.476168	0.420121	0.460678	0.457101	0.338303	0.407069	0.118968
Xie-Beni	minimum	17.576710	30.14763	13.40604	28.07055	10.17403	18.34990	87.07315

**Table 6.** Cluster evaluation details for dataset 2.

Index	Rule	k-means	k-medoids	CLARA	FCM	AGNES	DIANA	EM
Ball-Hall	maximum difference	412.059	408.698	419.786	413.067	1251.769	1620.499	1687.000
Banfeld-Raftery	minimum	5754.738	5746.353	5762.442	5753.021	7146.294	7034.551	7310.028
С	minimum	0.062866	0.065830	0.070027	0.063380	0.390822	0.313280	0.387854
Calinski-Harabasz	maximum	1338.7110	1322.6970	1290.2630	1333.2070	91.7943	147.9322	32.5353
Davies-Bouldin	minimum	0.829626	0.850951	0.872814	0.844661	4.241983	5.656803	5.532857
Det Ratio	minimum difference	-9.6247	9.3921	9.0682	-9.5368	-9.4520	-25.2786	4.4471
Dunn	maximum	0.010938	0.016630	0.009694	0.009391	0.004871	0.004938	0.004503
Baker-Hubert Gamma	maximum	0.816273	0.808407	0.795785	0.814896	0.165908	0.291998	0.107332
G plus	minimum	0.036715	0.037223	0.039204	0.036508	0.208229	0.174128	0.173479
GDI	maximum	0.010938	0.016630	0.009694	0.009391	0.004871	0.004938	0.004503
GDI	maximum	0.083379	0.123971	0.075915	0.070381	0.038030	0.038888	0.044819
GDI	maximum	0.029635	0.044156	0.027170	0.025084	0.014129	0.014456	0.015599
GDI	maximum	0.865136	0.841024	0.684735	0.865136	0.550273	0.896060	0.914911
GDI	maximum	6.595021	6.269512	5.362181	6.483784	4.296002	7.057368	9.106571
GDI	maximum	2.344042	2.233076	1.919110	2.310841	1.596043	2.623395	3.169596
GDI	maximum	0.348413	0.337470	0.307879	0.349650	0.202104	0.216721	0.188625
GDI	maximum	2.655986	2.515712	2.411012	2.620460	1.577830	1.706897	1.877479
GDI	maximum	0.944007	0.896047	0.862895	0.933940	0.586193	0.634495	0.653468
GDI	maximum	0.319263	0.295566	0.268033	0.308509	0.049881	0.036296	0.043258
GDI	maximum	2.433774	2.203327	2.098970	2.312131	0.389426	0.285867	0.430568
GDI	maximum	0.865027	0.784781	0.751216	0.824051	0.144679	0.106264	0.149862
GDI	maximum	0.123927	0.123076	0.117667	0.125257	0.130287	0.132107	0.128966
GDI	maximum	0.944711	0.917482	0.921449	0.938741	1.017159	1.040471	1.283662
GDI	maximum	0.335775	0.326789	0.329784	0.334570	0.377893	0.386769	0.446786

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Ksq DetW	maximum difference	8.52.E+19	-8.73.E+19	-9.04.E+19	8.60.E+19	8.67.E+19	3.24.E+19	-1.84.E+20
Log Det Ratio	minimum difference	NaN	2195.069	2160.676	NaN	NaN	NaN	1462.398
Log SS Ratio	minimum difference	1.414612	1.402578	1.377751	1.410492	-1.265300	-0.788096	-2.302524
McClain-Rao	minimum	0.367882	0.370062	0.375365	0.367628	0.813124	0.708248	0.914219
PBM	maximum	4654.983	4288.195	4032.787	4472.888	374.272	239.935	80.346
Point-Biserial	maximum	-17.95063	-17.46502	-17.12382	-17.76397	-5.38039	-8.69440	-2.02907
Ray-Turi	minimum	0.253663	0.298844	0.323877	0.272556	12.228300	21.023680	14.771200
Ratkowsky-Lance	maximum	0.218594	0.217163	0.216372	0.217995	0.243366	0.292046	0.141017
Scott-Symons	minimum	NaN	NaN	NaN	NaN	NaN	NaN	NaN
SD	minimum	0.173550	0.173544	0.178539	0.174266	0.629842	0.835184	0.898221
SD	minimum	0.065546	0.071095	0.073397	0.067935	0.239807	0.286920	0.201936
S Dbw	minimum	2.160563	2.334583	1.959573	2.304092	4.564995	6.526231	7.487439
Silhouette	maximum	0.385259	0.371411	0.353295	0.377094	0.076218	-0.058792	0.029971
Tau	maximum	0.516042	0.503921	0.493095	0.511805	0.117232	0.204792	0.066915
Trace W	maximum difference	369788.7	373381.8	380877.8	371015.8	1475195.0	1300210.0	1719471.0
Trace WiB	maximum difference	8.475324	8.189494	7.884873	8.338135	4.168003	6.162842	2.878671
Wemmert-Gan carski	maximum	0.520069	0.514221	0.497763	0.516158	0.001709	0.000000	0.008162
Xie-Beni	minimum	216.125400	94.39833	247.59490	294.15460	1282.19600	1136.05800	1363.25800

**Table 7.** Cluster evaluation details for dataset 3.

Ball-Hall         maximum difference minimum         16980.860         17880.530         22.290         24.320         22.069         25.389         24.444         23.157           Banfeld-Raftery         minimum         16980.860         1780.530         17380.240         -Inf         18250.960         1684.940         17418.150           Calinski-Harabasz         maximum         550.3073         507.4880         450.7393         470.4533         261.5554         395.6296         386.4883           Davies-Bouldin         minimum         1.05948         2.134367         2.500716         1.965875         2.10152         2.020829         2.834875           Dunn         maximum         0.005693         0.010780         0.007623         0.010134         0.080888         0.12356         0.484171           G plus         minimum         0.035017         0.046522         0.047721         0.143781         0.118860         0.01235         0.045032           GDI         maximum         0.005693         0.010780         0.007623         0.001034         0.08888         0.012356         0.03451           GDI         maximum         0.024223         0.013590         0.025977         0.011574         0.014018         0.08803         0.012356	Index	Rule	lr maana	k-medoids	CLARA	FCM	AGNES	DIANA	EM
Banfeld-Raftery			k-means						
C         minimum         0.151689         0.201555         0.201569         0.263825         0.21935         0.21888         0.287825         0.23825         0.23825         0.23825         0.23825         0.23825         0.23825         0.23824         0.24487         0.23557         0.62452         0.424875         0.23557         0.62452         0.43824         0.007623         0.001344         0.03835         0.023418         0.03835         0.023417         0.01344         0.03835         0.023418         0.034256         0.03424         0.03835         0.02341         0.04418         0.03236         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435         0.03435									
Calinski-Harabasz	•								
Davies-Bouldin Der Ratio         minimum difference in Minimum difference in Mak.8010         4.15.754         3.56.1966         4.6127         676.4823         2.020829         2.834873         184.1171         Dunn maximum maximum (0.00569)         3.010780         3.001034         4.6127         676.4823         2.88.4327         184.1171         2.001034         0.008685         0.001330         2.004521         0.001634         0.008685         0.012336         0.034818           Baker-Hubert Gamma         maximum         0.023510         0.004622         0.047211         0.143781         0.11866         0.07217         0.072640           GDI         maximum         0.005693         0.010780         0.007623         0.001034         0.080885         0.012336         0.034881           GDI         maximum         0.007825         0.013596         0.009957         0.001374         0.103715         0.015256         0.04717           GDI         maximum         0.088649         0.95520         0.911923         0.697276         0.917979         0.978892         0.63719           GDI         maximum         1.28021         1.218263         1.91174         0.96316         1.177476         1.23225         0.92861           GDI         maximum         1.254980									
Det Ratio         minimum difference         148,8010         618,5754         356,1966         4,6127         676,4823         288,4327         184,1171           Dunn         maximum         0,005693         0,001768         0,007623         0,001034         0,008588         0,01236         0,043709           G plus         minimum         0,033017         0,046522         0,047721         0,143781         0,118866         0,072171         0,07240           GDI         maximum         0,002593         0,010359         0,008301         0,009957         0,01034         0,008388         0,012350         0,034981           GDI         maximum         0,007825         0,013596         0,009957         0,011374         0,103715         0,040101         0,04101         0,04171           GDI         maximum         0,86049         0,965920         0,911923         0,697276         0,197799         0,79892         0,681791           GDI         maximum         0,349016         3,435305         3,386773         2,632919         3,51862         3,493016         2,66612           GDI         maximum         0,51969         0,509647         0,546404         0,476518         0,579490         0,57973         0,445269									
Dunn         maximum         0.005693         0.010780         0.007623         0.001034         0.080858         0.012350         0.034818           Baker-Hubert Gamus         maximum         0.723710         0.046286         0.625110         0.424875         0.52557         0.62652         0.437096           GDI         minimum         0.005693         0.010780         0.007623         0.001034         0.080858         0.012345         0.03481           GDI         maximum         0.002422         0.038339         0.028310         0.009905         0.29241         0.04018         0.135730           GDI         maximum         0.0886049         0.965920         0.911923         0.697276         0.91797         0.78892         0.68171           GDI         maximum         0.486049         0.965920         0.911923         0.69276         0.91797         0.978892         0.68171           GDI         maximum         1.280017         2.181263         0.39187         0.92616         0.91797         0.546612         0.91797         0.73801         0.68112           GDI         maximum         1.21696         0.509647         0.546404         0.476518         0.579940         0.597573         0.442299									
Baker-Hubert Garms         maximum         0.723710         0.602866         0.625110         0.424875         0.523657         0.624652         0.43708           G plus         minimum         0.0035017         0.0046522         0.001723         0.001734         0.003868         0.072171         0.072640           GDI         maximum         0.0072423         0.038393         0.028310         0.003905         0.295241         0.044018         0.133730           GDI         maximum         0.007825         0.015596         0.009957         0.019173         0.015756         0.047017           GDI         maximum         0.349016         3.435305         3.386773         2.632919         3.51862         3.93016         2.636612           GDI         maximum         0.21606         0.509647         0.546404         0.476518         0.57990         0.97892         0.266612           GDI         maximum         0.218069         0.50947         0.546404         0.476518         0.57990         0.37525         0.292088           GDI         maximum         0.274980         0.642790         0.713725         0.652779         0.743880         0.75210         0.65401           GDI         maximum         0.296736									
G plus         minimum         0.033017         0.046522         0.047721         0.143781         0.118866         0.072171         0.072640           GDI         maximum         0.005693         0.010380         0.000383         0.013350         0.034581           GDI         maximum         0.007825         0.013596         0.009957         0.001374         0.103715         0.015526         0.047017           GDI         maximum         0.886049         0.965920         0.911923         0.697276         0.917979         0.978892         0.681791           GDI         maximum         3.490176         3.455305         3.386773         2.63291         3.351862         3.495016         2.636612           GDI         maximum         0.521696         0.509647         0.546404         0.476318         0.57990         0.59773         0.445269           GDI         maximum         2.054980         1.812563         2.029278         1.778582         2.117565         0.52779         0.743880         0.552101         0.604501           GDI         maximum         0.717159         0.642790         0.713725         0.652779         0.743880         0.752101         0.65361           GDI         maximum         0.0									
GDI         maximum         0.005693         0.010780         0.007623         0.001034         0.08858         0.012336         0.035730           GDI         maximum         0.002423         0.088310         0.005905         0.0295241         0.044018         0.137373           GDI         maximum         0.086049         0.965920         0.911923         0.697276         0.917979         0.97882         0.681791           GDI         maximum         3.49016         3.455305         3.386773         2.632919         3.551862         3.49016         2.66612           GDI         maximum         0.521696         0.509647         0.546404         0.476518         0.579940         0.597573         0.445269           GDI         maximum         0.251696         0.509647         0.546404         0.476518         0.579790         0.597573         0.445269           GDI         maximum         0.711759         0.642790         0.713725         0.632779         0.743880         0.752101         0.65401           GDI         maximum         0.706756         0.292915         0.766836         1.16354         1.008565         1.165340         0.594814           GDI         maximum         0.382745         0.32945									
GDI         maximum         0.022423         0.038339         0.028310         0.030905         0.29241         0.04018         0.13370           GDI         maximum         0.007825         0.015960         0.009957         0.01374         0.101575         0.015705         0.04707           GDI         maximum         3.49016         3.435305         3.38673         2.632919         3.351862         3.493016         2.636612           GDI         maximum         1.218022         1.218263         1.191174         0.926316         1.17746         1.232025         0.246846           GDI         maximum         2.054980         1.812563         2.029278         1.798582         2.117655         2.152342         1.721935           GDI         maximum         0.717159         0.642790         0.713725         0.632779         0.743880         0.752101         0.65401           GDI         maximum         0.708736         0.292015         0.766836         1.163354         1.008565         1.165381           GDI         maximum         0.284736         0.278561         0.293977         0.320391         0.276201         0.352592         0.217224           GDI         maximum         0.1284736         0.278561<	•								
GDI         maximum         0.007825         0.013596         0.009957         0.001374         0.103715         0.01526         0.047017           GDI         maximum         0.886049         0.965920         0.911923         0.697276         0.917979         0.978892         0.681791           GDI         maximum         1.218022         1.218263         1.191174         0.926516         1.177476         1.232025         0.926984           GDI         maximum         0.521696         0.509647         0.546404         0.476518         0.579940         0.597573         0.445269           GDI         maximum         0.171759         0.642790         0.713725         0.632779         0.743880         0.752101         0.65401           GDI         maximum         0.171759         0.642790         0.713725         0.632779         0.743880         0.752101         0.65401           GDI         maximum         1.096736         0.292015         0.766836         1.163554         1.008565         1.165340         0.594814           GDI         maximum         1.038745         0.329457         0.269707         0.40929         0.534329         0.41102         0.594814           GDI         maximum         0.3141									
GDI         maximum         0.886049         0.965920         0.911923         0.697276         0.917979         0.978892         0.681791           GDI         maximum         3.490176         3.455305         3.366773         2.632919         3.351862         3.493016         2.636612           GDI         maximum         0.521696         0.509647         0.546404         0.476518         0.579940         0.597573         0.445269           GDI         maximum         2.054980         1.812563         2.029278         1.798582         2.117565         2.132342         1.721935           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.526578         0.153811           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.326578         0.153811           GDI         maximum         0.382745         0.329457         0.266970         0.409292         0.354299         0.411028         0.29126           GDI         maximum         0.328476         0.278561         0.295777         0.352395         0.260646         0.325292         0.217224           GDI         maximum         0.									
GDI         maximum         3.490176         3.455305         3.586773         2.632919         3.351862         3.493016         2.636612           GDI         maximum         1.218022         1.218263         1.191174         0.926316         1.177476         1.232025         0.926984           GDI         maximum         0.521696         0.509647         0.546404         0.476318         0.579940         0.597573         0.445269           GDI         maximum         0.2054980         1.812563         2.029278         1.798582         2.117565         2.132342         1.721935           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.776217         0.326578         0.155811           GDI         maximum         1.0976736         0.229457         0.266707         0.409292         0.354299         0.411028         0.209126           GDI         maximum         1.038745         0.329457         0.269707         0.409292         0.354299         0.411028         0.209126           GDI         maximum         1.211586         0.990706         1.091796         1.330648         0.951711         1.160751         0.480404           KSQ         DEM         max									
GDI         maximum         1.218022         1.218263         1.91174         0.926316         1.177476         1.232025         0.926984           GDI         maximum         0.521696         0.509647         0.546404         0.476318         0.579940         0.597573         0.445269           GDI         maximum         2.054980         1.812563         2.029278         1.798582         2.117565         2.132342         1.71935           GDI         maximum         0.717159         0.642790         0.713725         0.632779         0.743880         0.752101         0.605401           GDI         maximum         1.096736         0.929015         0.766836         1.163354         1.008565         1.165340         0.594814           GDI         maximum         0.284736         0.229577         0.269707         0.409292         0.36664         0.325292         0.217224           GDI         maximum         0.284736         0.299076         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum difference         2.67.E+89         0.4997076         1.091796         1.353048         0.951711         1.160751         0.840044           GDI         maximum differen									
GDI         maximum         0.521696         0.509647         0.546404         0.476318         0.579940         0.597573         0.445269           GDI         maximum         2.054980         1.812563         2.029278         1.798582         2.117565         2.132342         1.721935           GDI         maximum         0.717159         0.642790         0.713725         0.632779         0.743880         0.752101         0.605401           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.356784         0.153811           GDI         maximum         0.382745         0.329457         0.269707         0.409292         0.354299         0.411028         0.29126           GDI         maximum         0.382745         0.2278561         0.293977         0.352395         0.260646         0.325292         0.217224           GDI         maximum         0.381417         0.551334         0.384000         0.468150         0.354326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log SS Ratio									
GDI         maximum         2.054980         1.812563         2.029278         1.798582         2.117565         2.132342         1.721935           GDI         maximum         0.717159         0.642790         0.713725         0.632779         0.743880         0.752101         0.605401           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.326578         0.158311           GDI         maximum         0.382745         0.299015         0.766836         1.163534         1.008565         1.165340         0.594814           GDI         maximum         0.382745         0.278561         0.293977         0.352395         0.260646         0.325292         0.217224           GDI         maximum         0.28117         0.351334         0.384000         0.468150         0.334326         0.49110         0.295344           KSq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log Det Ratio         minimum difference         39852.710         35068.00         31741.350         8341.192         5.87.E+89         1.38.E+90         2.16.E+90		maximum	1.218022		1.191174	0.926316			0.926984
GDI         maximum         0.717159         0.642790         0.713725         0.632779         0.743880         0.752101         0.605401           GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.326578         0.153811           GDI         maximum         1.096736         0.29915         0.766836         1.163354         1.008565         1.165340         0.594814           GDI         maximum         0.382745         0.329457         0.269707         0.409292         0.352499         0.411028         0.209126           GDI         maximum         0.284736         0.278561         0.293977         0.352395         0.260464         0.325292         0.217224           GDI         maximum         1.211586         0.990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum         0.331417         0.351334         0.384000         0.468150         0.334326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.486160         0.68163         0.82556.24		maximum	0.521696	0.509647			0.579940	0.597573	0.445269
GDI         maximum         0.278428         0.261215         0.206479         0.308091         0.276217         0.326578         0.153811           GDI         maximum         1.096736         0.929015         0.766836         1.163354         1.008565         1.165340         0.594814           GDI         maximum         0.284736         0.2278561         0.269707         0.409292         0.354299         0.411028         0.201224           GDI         maximum         0.284736         0.2990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum         0.391417         0.351334         0.384000         0.468150         0.334326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log SS Ratio         minimum difference         39852.710         35068.000         31741.350         8341.192         35556.240         3095.300         28456.160           Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681683         -0.69992		maximum			2.029278				1.721935
GDI         maximum         1.096736         0.929015         0.766836         1.163354         1.008565         1.165340         0.594814           GDI         maximum         0.382745         0.329457         0.269707         0.409292         0.354299         0.411028         0.209126           GDI         maximum         0.284736         0.278561         0.293977         0.352395         0.260646         0.325292         0.217224           GDI         maximum         1.121586         0.990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90         2.16.E+90         0.42610         0.34341         5.87.E+89         1.38.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90         0.42610         0.427621         0.546205         -1.757077         -1.091213         -0.681683         -0.699992           McClain-Rao         minimum         0.717476         0.759115         0.758793         0.852714         0.824172         0.777429         0.822768           PBM         maximum         -0.87507         -0.73370	GDI	maximum	0.717159	0.642790	0.713725	0.632779	0.743880	0.752101	0.605401
GDI         maximum         0.382745         0.329457         0.269707         0.409292         0.354299         0.411028         0.209124           GDI         maximum         0.284736         0.278561         0.293977         0.352395         0.260646         0.325292         0.217224           GDI         maximum         1.121586         0.990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum difference         2.67.E489         6.42.E489         1.18.E490         1.21.E491         5.87.E489         1.38.E490         2.16.E490           Log Det Ratio         minimum difference         39852.710         35068.000         31741.350         8341.192         35556.240         30905.300         28456.160           Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681683         -0.699992           McClain-Rao         minimum         0.717476         0.759115         0.758793         0.852714         0.824172         0.777429         0.822768           PBM         maximum         2.08550         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328	GDI	maximum	0.278428	0.261215	0.206479	0.308091	0.276217	0.326578	0.153811
GDI         maximum         0.284736         0.278561         0.293977         0.352395         0.260646         0.325292         0.217224           GDI         maximum         1.121586         0.990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum         0.391417         0.351334         0.384000         0.468150         0.334326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log Det Ratio         minimum difference         39852.710         35068.000         31741.550         8341.192         3556.240         30905.300         28456.160           Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681638         -0.699992           McClain-Rao         minimum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           Point-Biserial         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328	GDI	maximum	1.096736	0.929015	0.766836	1.163354	1.008565	1.165340	0.594814
GDI         maximum         1.121586         0.990706         1.091796         1.330648         0.951711         1.160751         0.840044           GDI         maximum         0.391417         0.351334         0.384000         0.468150         0.334326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log Det Ratio         minimum difference         39852.710         35068.000         31741.350         8341.192         35556.240         30905.300         28456.160           Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681683         -0.699992           McClain-Rao         minimum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           PBM         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012	GDI	maximum			0.269707				0.209126
GDI         maximum         0.391417         0.351334         0.384000         0.468150         0.334326         0.409410         0.295344           Ksq DetW         maximum difference         2.67.E+89         6.42.E+89         1.18.E+90         1.21.E+91         5.87.E+89         1.38.E+90         2.16.E+90           Log Det Ratio         minimum difference         39852.710         35068.000         31741.350         8341.192         35556.240         30905.300         28456.160           Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681683         -0.699992           McClain-Rao         minimum         0.717476         0.759115         0.758793         0.852714         0.824172         0.777429         0.822768           PBM         maximum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           Point-Biserial         maximum         -0.87507         -0.75370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.34609         4.359012	GDI	maximum	0.284736	0.278561	0.293977	0.352395	0.260646	0.325292	0.217224
Ksq DetWmaximum difference2.67.E+896.42.E+891.18.E+901.21.E+915.87.E+891.38.E+902.16.E+90Log Det Ratiominimum difference39852.71035068.00031741.3508341.19235556.24030905.30028456.160Log SS Ratiominimum difference-0.346617-0.427621-0.546205-1.757077-1.091213-0.681683-0.699992McClain-Raominimum0.7174760.7591150.7587930.8527140.8241720.7774290.822768PBMmaximum2.2632.3422.6123.3012.4232.5282.211Point-Biserialmaximum-0.87507-0.73370-0.76860-0.68436-0.82559-0.89172-0.56328Ray-Turiminimum1.3894541.8302322.9607011.4486981.8702341.3464094.359012Ratkowsky-Lancemaximum0.2238880.2134390.2081740.2132760.1928580.2089250.201579Scott-SymonsminimumNaNNaNNaN-InfNaNNaNNaNSDminimum0.7687060.6855680.7373990.6082740.8397760.8266520.811169SDminimumNaNNaNNaNNaNNaNNaNNaNSilhouettemaximum0.1498960.1388250.129434NaN0.1586460.1631840.132553Taumaximum difference123845.9127970.2133879.1180303.3158266.914		maximum	1.121586	0.990706	1.091796	1.330648	0.951711	1.160751	0.840044
Log Det Ratiominimum difference39852.71035068.00031741.3508341.19235556.24030905.30028456.160Log SS Ratiominimum difference-0.346617-0.427621-0.546205-1.757077-1.091213-0.681683-0.699992McClain-Raominimum0.7174760.7591150.7587930.8527140.8241720.7774290.822768PBMmaximum2.2632.3422.6123.3012.4232.5282.211Point-Biserialmaximum-0.87507-0.73370-0.76860-0.68436-0.82559-0.89172-0.56328Ray-Turiminimum1.3894541.8302322.9607011.4486981.8702341.3464094.359012Ratkowsky-Lancemaximum0.2238880.2134390.2081740.2132760.1928580.2089250.201579Scott-SymonsminimumNaNNaNNaN-InfNaNNaNNaNSDminimum0.7687060.6855680.7373990.6082740.8397760.8266520.811169SDminimumNaNNaNNaNNaNNaNNaNNaNSilhouettemaximum0.1498960.1388250.129434NaN0.1586460.1631840.132553Taumaximum difference123845.9127970.2133879.1180303.3158266.9140403.3141264.1Trace WiBmaximum difference16.28745012.41211010.9431203.60337313.8192900.21	GDI	maximum	0.391417	0.351334	0.384000	0.468150	0.334326	0.409410	0.295344
Log SS Ratio         minimum difference         -0.346617         -0.427621         -0.546205         -1.757077         -1.091213         -0.681683         -0.699992           McClain-Rao         minimum         0.717476         0.759115         0.758793         0.852714         0.824172         0.777429         0.822768           PBM         maximum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           Point-Biserial         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012           Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           S Dbw         minimum<	Ksq DetW	maximum difference	2.67.E+89	6.42.E+89	1.18.E+90	1.21.E+91	5.87.E+89	1.38.E+90	2.16.E+90
McClain-Rao         minimum         0.717476         0.759115         0.758793         0.852714         0.824172         0.777429         0.822768           PBM         maximum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           Point-Biserial         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012           Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         NaN         0.158646	Log Det Ratio	minimum difference	39852.710	35068.000	31741.350	8341.192	35556.240	30905.300	28456.160
PBM         maximum         2.263         2.342         2.612         3.301         2.423         2.528         2.211           Point-Biserial         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012           Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         0.158646         0.163184         0.13	Log SS Ratio	minimum difference	-0.346617	-0.427621	-0.546205	-1.757077	-1.091213	-0.681683	-0.699992
Point-Biserial         maximum         -0.87507         -0.73370         -0.76860         -0.68436         -0.82559         -0.89172         -0.56328           Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012           Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         0.158646         0.163184         0.132553         0.222056         Tase         Tase         maximum difference         123845.9         127970.2<	McClain-Rao	minimum	0.717476	0.759115	0.758793	0.852714	0.824172	0.777429	0.822768
Ray-Turi         minimum         1.389454         1.830232         2.960701         1.448698         1.870234         1.346409         4.359012           Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         0.158646         0.163184         0.132553         0.222056         Tau         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB<	PBM	maximum	2.263	2.342	2.612	3.301	2.423	2.528	2.211
Ratkowsky-Lance         maximum         0.223888         0.213439         0.208174         0.213276         0.192858         0.208925         0.201579           Scott-Symons         minimum         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         0.158646         0.163184         0.132553           Tau         maximum         0.353806         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290	Point-Biserial	maximum	-0.87507	-0.73370	-0.76860	-0.68436	-0.82559	-0.89172	-0.56328
Scott-Symons         minimum         NaN         NaN         NaN         -Inf         NaN         NaN         NaN           SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         0.158646         0.163184         0.132553         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728 <td>Ray-Turi</td> <td>minimum</td> <td>1.389454</td> <td>1.830232</td> <td>2.960701</td> <td>1.448698</td> <td>1.870234</td> <td>1.346409</td> <td>4.359012</td>	Ray-Turi	minimum	1.389454	1.830232	2.960701	1.448698	1.870234	1.346409	4.359012
SD         minimum         0.768706         0.685568         0.737399         0.608274         0.839776         0.826652         0.811169           SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         NaN         NaN         NaN         NaN         NaN         NaN         NaN         NaN         0.158646         0.163184         0.132553           Tau         maximum         0.353806         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	Ratkowsky-Lance	maximum	0.223888	0.213439	0.208174	0.213276	0.192858	0.208925	0.201579
SD         minimum         0.418255         0.505083         0.652722         0.320192         0.482594         0.398025         0.786303           S Dbw         minimum         NaN         NaN         NaN         NaN         NaN         NaN         NaN         NaN         0.158646         0.163184         0.132553           Silhouette         maximum         0.449896         0.138825         0.129434         NaN         0.158646         0.163184         0.132553           Tau         maximum         0.553806         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	Scott-Symons	minimum	NaN	NaN	NaN	-Inf	NaN	NaN	NaN
S Dbw         minimum         NaN         N	SD	minimum	0.768706	0.685568	0.737399	0.608274	0.839776	0.826652	0.811169
Silhouette         maximum         0.149896         0.138825         0.129434         NaN         0.158646         0.163184         0.132553           Tau         maximum         0.353806         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	SD	minimum	0.418255	0.505083	0.652722	0.320192	0.482594	0.398025	0.786303
Tau         maximum         0.353806         0.291808         0.315408         0.300432         0.369940         0.387363         0.222056           Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	S Dbw	minimum	NaN	NaN	NaN	NaN	NaN	NaN	NaN
Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	Silhouette	maximum		0.138825	0.129434		0.158646		
Trace W         maximum difference         123845.9         127970.2         133879.1         180303.3         158266.9         140403.3         141264.1           Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	Tau	maximum		0.291808	0.315408	0.300432	0.369940	0.387363	0.222056
Trace WiB         maximum difference         16.287450         12.412110         10.943120         3.603373         13.819290         12.616240         9.776459           Wemmert-Gan carski         maximum         0.238891         0.224468         0.180752         0.190689         0.204696         0.211226         0.138728	Trace W	maximum difference		127970.2	133879.1				141264.1
Wemmert-Gan carski maximum 0.238891 0.224468 0.180752 0.190689 0.204696 0.211226 0.138728		maximum difference							
Xie-Beni minimum 3323 916000 1074 63400 2172 26900 128586 70000 21 82478 943 66480 86 23692	Wemmert-Gan carsk								0.138728
7110 Delli illillillilli 3323,710000 1071,03100 2172,20700 120300,70000 21,02470 743,00400 00,23072	Xie-Beni	minimum	3323.916000	1074.63400	2172.26900	128586.70000	21.82478	943.66480	86.23692

#### Silhouette index

The Silhouette Index (SI) is a cluster evaluation criterion which represents the quality of clustering by indicating how well the elements in the dataset is clustered (Rousseeuw, 1987). Alternatively, it indicates how similar an element is to the cluster it belongs to. A high value for SI is considered as a result of good clustering. Mathematically, Silhouette Index is calculated as the mean of the mean Silhouette (10) of all the clusters as in Equation (14).

$$S.I. = \frac{1}{\nu} \sum_{k=1}^{K} S_k \tag{14}$$

Figure 12 represents evaluation of multiple clustering algorithms on all three datasets considered in this paper using Silhouette Index.

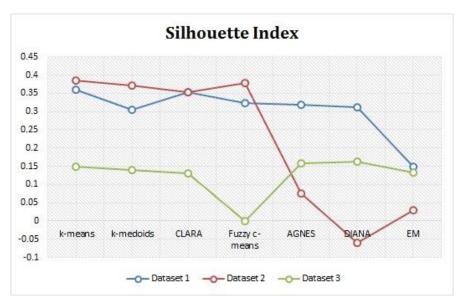


Figure 12. Evaluation of clustering algorithms using Silhouette Index.

## **Dunn index**

Dunn Index (DI) is an internal cluster evaluation metric described as the ratio of minimum inter-cluster separation to maximum intra-cluster distance (Dunn, 1973). Mathematically, it can be arrived through steps Equation (15) to (19). The distance between two clusters  $C_k$  and  $C_k$ , can be represented by the distance between their closest points.

$$d_{kk'} = \min_{i \in I_k \text{ and } j \in I_{k'}} \left| \left| E_i^{\{k\}} - E_j^{\{k'\}} \right| \right|$$
 (15)

The inter-cluster separation can be computed as the minimum of the pairwise distance.

$$d_{\min} = \min_{k \neq k'} d_{kk'} \tag{16}$$

The largest distance separating two points within a cluster (also referred as diameter of the cluster) can be calculates as below:

$$D_k = \max_{i,j \in I_k \text{ and } i \neq j} \left| \left| E_i^{\{k\}} - E_j^{\{k\}} \right| \right|$$
 (17)

The intra-cluster compactness is computed as the maximum value of intra-cluster distances.

$$d_{\max} = \max_{1 \le k \le K} D_k \tag{18}$$

Dunn index can be represented as the ratio between inter-cluster separation and intra-cluster compactness.

$$D.I. = \frac{d_{\min}}{d_{\max}} \tag{19}$$

Figure 13 represents evaluation of multiple clustering algorithms on all three datasets considered in this paper using Dunn Index.

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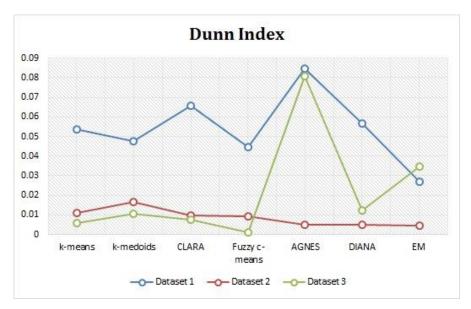


Figure 13. Evaluation of clustering algorithms using Dunn Index.

#### Calinski-Harabasz index

The Calinski-Harabasz Index (CHI) is an internal cluster evaluation measure expressed as the ratio of intercluster dispersion (variance between clusters) and intra-cluster dispersion (variance within each cluster) (Calinski & Harabasz, 1974). A larger value for Calinski-Harabasz Index is considered as the indication of good clustering. Mathematically, Calinski-Harabasz Index is calculated through steps Equation (20) to (23).

The inter-cluster dispersion can be defined as the dispersion of cluster centroids,  $G^{\{k\}}$  with respect to the global centroid, G of the dataset in consideration. If  $n_k$  is the number of elements in the cluster,  $C_k$ ,.

$$BCD = \sum_{k=1}^{K} n_k \left| \left| G^{\{k\}} - G \right| \right|^2$$
 (20)

The intra-cluster dispersion of cluster  $C_k$  is the sum of the squared distances between its elements,  $E_i^{\{k\}}$  and the cluster centrod,  $G^{\{k\}}$ .

$$WCD^{\{k\}} = \sum_{i \in I_k} \left| \left| E_i^{\{k\}} - G^{\{k\}} \right| \right|^2 \tag{21}$$

Hence, the pooled intra-cluster dispersion can be explained as the sum of the intra-cluster dispersions of all the clusters

$$WCD = \sum_{k=0}^{K} WCD^{\{k\}}$$
 (22)

Calinski-Harabasz Index is calculated as the ratio of BCD and WCD.

$$C.H.I. = \frac{\frac{BCD}{(K-1)}}{\frac{WCD}{(N-K)}} = \frac{(N-K)}{(K-1)} \frac{BCD}{WCD}$$

$$(23)$$

Figure 14 represents evaluation of multiple clustering algorithms on all three datasets considered in this paper using Calinski-Harabasz Index.

#### **Davies-Bouldin index**

The Davies-Bouldin Index (DBI) is a measure to evaluate cluster quality as it attempts to detect group of clusters that are well separated and compact by calculating the ratio of intra-cluster distances to inter-cluster distances (Davies & Bouldin, 1979). A smaller value for DBI represents better quality of clustering. Mathematically, Davies-Bouldin Index is calculated through steps Equation (24) to (26).

Calculate the mean distance,  $\delta_k$  of the elements in cluster  $C_k$  to its centroid,  $H^{\{k\}}$ .

$$\delta_k = \frac{1}{n_k} \sum_{i \in I_k} \left| \left| M_i^{\{k\}} - H^{\{k\}} \right| \right|$$
 (24)

The distance between centroids  $H^{\{k\}}$  and  $H^{\{k'\}}$  of clusters  $C_k$  and  $C_{k'}$  is computed as

$$\Delta_{kk'} = d(H^{\{k\}}, H^{\{k'\}}) = \left| \left| H^{\{k'\}} - H^{\{k\}} \right| \right|$$
 (25)

For each cluster,  $C_k$  identify the maximum,  $M_k$  of  $\frac{\delta_k + \delta_{k'}}{\Delta_{kk'}}$  for all  $k' \neq k$ .

Davies-Bouldin Index is the mean value of  $M_k$  aong all the clusters in the dataset in consideration.

$$D.B.I. = \frac{1}{K} \sum_{k=1}^{K} M_k = \frac{1}{K} \sum_{k=1}^{K} \max_{k' \neq k} \left( \frac{\delta_k + \delta_{k'}}{\delta_{kk'}} \right)$$
 (26)

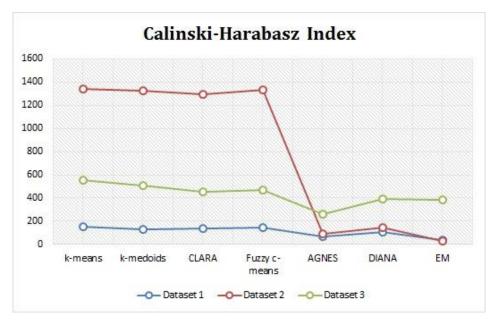


Figure 14. Evaluation of clustering algorithms using Calinski-Harabasz Index.

Figure 15 represents evaluation of multiple clustering algorithms on all three datasets considered in this paper using Davies-Bouldin Index.

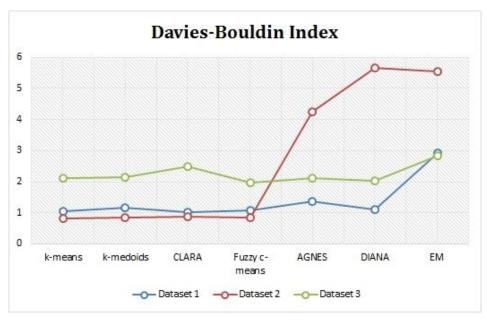


Figure 15. Evaluation of clustering algorithms using Davies-Bouldin Index.

## Discussion

In this experiment, we referred to three real datasets covering numerical information extracted from reviews, feedbacks, and ratings from travelers that are collated from holidayiq.com, tripadvisor.com, and Google destination reviews, respectively. As part of the empirical analysis, we evaluated seven core clustering algorithms using internal evaluation strategies. Our consideration included four partitioning clustering

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algorithms (k-means, k-medoids, CLARA, and Fuzzy c-means), two hierarchical clustering algorithms (AGNES, and DIANA) and one model-based clustering algorithm (EM).

We could observe that partitioning algorithms showed an edge with lower volume and a smaller number of attributes. However, no pattern is observed with larger volume of data and high number of attributes. So, we recommend evaluating and choosing an algorithm for the dataset to be processed rather than selecting an algorithm upfront. We introduced a structured and data driven approach in our analysis using defined and repeatable processes and is explained in section 4.1 which can be extended for evaluating clustering algorithms in similar contexts.

Another attribute which requires attention is the execution time required for various clustering algorithms. Though the execution time is highly dependent on the hardware configuration and environment variables used, it is also important to check the time complexity for various clustering algorithms. The cardinality and dimensionality of the dataset being processed have major influence on the overall processing time. We have conducted an explicit research on the same and the results are already published (Renjith, Sreekumar, & Jathavedan, 2020a).

## Conclusion

Clustering is considered as a key strategy for handling large volume of data generated in social media platforms. It helps to reduce the volume of data to be processed and thereby reducing the computational cost and processing time required. Any type of social media content that can be treated as the reflection of traveler traits and/or feedbacks can be considered as a tourism social media data.

In this experiment, we evaluated seven core clustering algorithms against three real datasets covering numerical information extracted from reviews, feedbacks, and ratings from travelers on holidayiq.com, tripadvisor.com, and Google destination reviews. Based on the results obtained, no algorithm could outperform in all tourism scenarios as performance varied against evaluation criteria chosen and dataset being considered. So, it is critical to evaluate and select appropriate clustering algorithms for each of the dataset to be processed.

Another cause for the high computational intensiveness of social media data is the curse of dimensionality. As a subsequent step of this work, we are planning to leverage dimensionality reduction techniques prior to clustering process. We aim to evaluate various dimensionality reduction techniques ranging from principal component analysis (PCA) to deep learning techniques like autoencoder against real data from tourism domain.

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